

# COLLISION PREVENTION PROTOCOL FOR A DYNAMIC GROUP OF ASYNCHRONOUS COOPERATIVE ROBOTS

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**Abstract.** The protocol is based on a fully distributed path reservation system. It assumes an ad hoc network formed by the mobile grippers of the robots, and takes advantage of the wireless communication. The protocol requires initial complete knowledge of the composition of the robots group. A performance analysis of the protocol provides insights for a correct dimensioning of system parameters in order to maximize the average effective speed of the robots' grippers.

**Keywords:** Collision prevention protocol, autonomous cooperative robots' grippers, distributed algorithms

## 1. Introduction

This paper extends work that was presented in the previous article "*Collision Prevention Method for a Dynamic Group of Cooperative Robots who Communicate Wirelessly*", recently proposed for **RECENT** journal. The main additions are that is presented a more rigorous specification for the collision prevention problem, and include proofs of correctness of the protocol and its properties.

The paper presents a collision prevention protocol for a dynamic group of cooperative robots' grippers with asynchronous communications. The protocol is based on a Neighbourhood Discovery Service (NDS), which is the only synchronous part of the system. Furthermore, although the communication range may be limited, no routing is needed as robots only communicate with their direct neighbourhood.

## 2. Locality-Preserving Protocol

A dynamic distributed system of robot-grippers,  $S = \{R_i\}$  is considered, in which each robot-gripper has a unique identifier where  $i$ , ( $1 \leq i \leq p$ ) denotes the index of dynamical systems comprising a network, and  $p$  is the total number of the individual elements.

The total composition of the system, of which the cooperative grippers group has only a partial knowledge, can change dynamically [1].

All cooperative grippers of the group run the same distributed algorithm. The algorithm consists of a distributed path reservation system, such that a gripper must reserve a zone before it moves. When a robot  $R_i$  requests a zone  $Z_i$  for her gripper,  $R_i$  must determine all the robots  $R_j$  that conflict with  $R_i$ . The robots  $R_j$  are located within one communication loop with respect to  $R_i$ , because the reservation range of the robots must be within half

of the transmission range [2].

A neighborhood discovery primitive (*NDiscover*) returns the set of neighbors  $Neighbor_i$  within one communication step with respect to  $R_i$ . Therefore,  $R_i$  can determine the set of robots  $R_j$  that conflict with  $R_i$ .  $R_i$  multicasts  $Z_i$  to the list of neighbors  $Neighbor_i$ , then  $R_i$  waits until it receives the response messages. Consequently,  $R_i$  determines the set of robots that it conflicts with. Intuitively,  $R_i$  performs a prudent negotiation with each of the robots that  $R_i$  conflicts with.

Therefore,  $R_i$  and each robot  $R_j$  decide consistently about the arrangement of their requests. So, a dynamic arrangement for the conflicting requests takes place. When  $R_i$  receives a release message from all the robots that  $R_i$  waits for, it reserves zone  $Z_i$  and becomes the owner of zone  $Z_i$ . After  $R_i$  has reached the post-motion zone,  $R_i$  releases zone  $Z_i$  except for the area occupied by  $R_i$ .

## 3. Protocol variables. Definitions and Terminology

Further the variables used by the collision prevention protocol are presented.

- *Paths*: Corridor denotes a bordering zone along which gripper of the robot moves. A path of a robot' gripper is a continuous route composed of a series of contiguous corridors.
- *Errors*: There are three sources of geometrical incertitude concerning the position and the motion of a robot' gripper. An error related to the position information provided by the positioning system is denoted  $e_{ps}$ . In addition, the motion of a robot creates two additional sources of errors. The first error is related to the translational movement, denoted  $e_{tr}$ . The second error is related to the rotational movement, denoted  $e_{ro}$ .

- *Moving zones*: The zone  $Z_i$  is composed of the following three parts, illustrated in figure 1. The first part, named pre-motion zone and denoted  $pre(Z_i)$ , is the zone that robot  $R_i$  possibly occupies while waiting (before moving). The second part,

named motion zone and denoted  $motion(Z_i)$ , is the zone that robot  $R_i$  possibly occupies while moving. The third part, named post-motion zone and denoted  $post(Z_i)$ , is the zone that robot  $R_i$  possibly reaches after the motion.

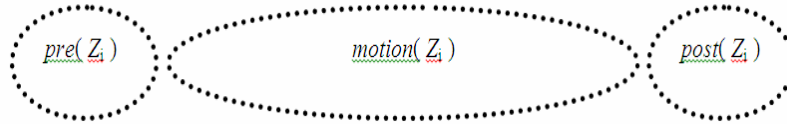


Fig. 1. Parts of the zone  $Z_i$

A moving zone is defined as the region needed by a robot's gripper to move safely along a corridor. This includes requirements for the shape of the robot, positioning error, and imprecision in the moving of the robot's gripper. The zone must have a convex shape and contain the corridor that robot's gripper rides.

- *zone*  $Z_i$  is the zone currently requested or owned by robot  $R_i$ .
- $Neighbor_i$  represents the set of robots that may possibly conflict with robot  $R_i$  (i.e., the output of the neighborhood discovery primitive  $NDiscover$ ).
- $G_i$  is a set of  $\{(R_j, Z_j)\}$  such that  $R_j$  belongs to  $Neighbor_i$ , and  $Z_j$  is the requested or the owned zone of  $R_j$ .  $Z_j$  intersects with the zone  $Z_i$ .
- $After_i$  is the list of robots waiting for  $R_i$  until it releases its zone.
- $Before_i$  is the list of robots that  $R_i$  waits for.
- $Depend_i$  is the dependency set. If a robot  $R_i$  requests the zone  $Z_i$  then it conflicts with a set of robots each of which conflicts with another set of robots and so on. The dependency set is the union of  $G_k$  for each robot  $R_k$  related to  $R_i$  by the transitive closure of the relation conflict.
- $Dag_{wait}$  is a wait-for delay such that  $R_i$  waits for  $R_j$  to release  $Z_j$ .
- $mssg$  is a message exchanged during the run of the protocol.

Each  $mssg$  message consists of three fields, the first is the type of the message which belongs to the set  $\{REQUEST, RELEASE, WAITFORME, ACK, PROHIBITED\}$ , the second field is the identifier of the robot sending the message, and the third field is the body of the message which consists of the specifications and the parameters of the requested (or owned) zone.

The type  $REQUEST$  denotes a request message;  $RELEASE$  denotes a release message, and the type  $WAITFORME$  means that the receiver of the message must wait for the sender. The type  $ACK$

indicates the sender and receiver do not conflict. The type  $PROHIBITED$  indicates that the receiver requests a zone that intersects with the pre-motion zone of the stationary sender, which does not move any more.

- Request  $pending_i$  is a boolean variable indicates that robot  $R_i$  has a requested zone and that  $R_i$  has determined its wait-for graph  $Dag_{wait}$ .

#### 4. Protocol phases

The phases of the protocol are explained with respect to a robot  $R_i$ . The robot  $R_i$  is located in the pre-motion zone  $pre(Z_i)$ . When robot the robot  $R_i$  requests a new zone  $Z_i$ , it proceeds as follows.

1) *Discovery phase*. The robot  $R_i$  calls the neighborhood discovery primitive  $NDiscover$ , to determine the set  $Neighbor_i$ . This set consists of robots  $R_j$ , that may possibly come in conflict with the robot  $R_i$  for the zone  $Z_i$ , since  $Z_j$  intersects with the circle centered on  $R_i$  with radius equals to the reservation range.

Neighborhood discovery primitive is a function that enables a robot to detect its local neighbors. These neighbors are within one communication loop and satisfy a certain known predefined condition.  $NDiscover$  primitive can be implemented as the traditional neighborhood discovery primitive of mobile ad hoc networks [3].

A contact message in a geographical region is centered on one gripper robot, at the time of calling  $NDiscover$ , with a radius within the transmission range. All the robots that receive the message and satisfy the predefined condition, acknowledge the caller of  $NDiscover$ .

2) *Negotiation phase*. The negotiation phase of the robot  $R_i$  starts by the determination of the set  $G_i$  which consists of the robots of  $Neighbor_i$  that conflict with the robot  $R_i$ . The output of the negotiation phase is the wait-for graph,  $Dag_{wait}$ .

Thus,  $R_i$  determines the set of robots that it waits for [4]. If the robot  $R_i$  receives a request from a robot  $R_k$  ( $Z_k$  intersects with the zone  $Z_i$ ) and  $R_k$  does not belong to  $G_i$ , then  $R_k$  must wait for the robot  $R_i$ .

The negotiation phase proceeds as follows.

- $R_i$  multicasts  $mssg_i = (REQUEST, i, Z_i)$  indicating that the robot  $R_i$  requests  $Z_i$  to all the members of  $Neighbor_i$  carrying the parameters of  $Z_i$ .

This multicast does not require any routing because the neighbors are located within one communication step with respect to the robot  $R_i$ .

- the robot  $R_i$  waits until it receives a response message  $mssg_j$  from each member of  $Neighbor_i$ .
- after the robot  $R_i$  has received the messages  $mssg_j$ , it determines the set of robots  $G_i$  that conflict with  $R_i$ . The set  $G_i$  is obtained from the received messages  $mssg_j$  after discarding the release messages  $mssg_j = (RELEASE, j, Z_j)$ , and discarding the request messages  $mssg_j = (REQUEST, j, Z_j)$  such that  $Z_j$  does not intersect with  $Z_i$ .

The set  $G_i$  contains two disjoint subsets of robots: the first subset denoted  $(G_1)_i$  is composed of robots  $R_j$  such that  $R_i$  does not belong to  $G_j$  (i.e.,  $R_i$  must wait for  $R_j$ ,  $R_j$  has sent the message  $mssg_j = (WAITFORME, j, Z_j)$ ). The second is the complementary subset denoted  $(G_2)_i$ , which is composed of robots  $R_j$  such that  $R_i$  belongs to  $G_j$ . Thus the robot  $R_i$  must wait for all the robots of  $(G_1)_i$ , in addition to a subset of  $(G_2)_i$ . This subset would be determined by the Conflict Resolver.

- the robot  $R_i$  determines the dependency set  $Depend_i$  by applying an Echo algorithm.

### Echo algorithm

The Echo algorithm is explained as follows: the robot  $R_i$  multicasts a token message to each robot that belongs to  $G_i$ . Upon receipt of the first message of the robot  $R_i$  by a robot  $R_k$  from  $R_j$  ( $R_j$  is called the father of  $R_k$ ), it multicasts the message of the robot  $R_i$  to all the robots of  $G_k$  except its father  $R_j$ . When a robot  $R_k$  has received the token message of the robot  $R_i$  from all the robots of  $G_k$ ,  $R_k$  adds the contents of  $G_k$  to the token message and sends it (echo) to the father  $R_j$ .

When the robot  $R_i$  has received the token message from all the robots of  $G_i$ , it obtains the dependency set. The dependency set is associated with the messages of type *WAITFORME*. The robot  $R_i$  computes the dependency set when it does not receive any *WAITFORME* message.

The motivation for building the dependency set is to enable the conflicting robots to build the wait-

for graph  $Dag_{wait}$  in a consistent manner and so to avoid cyclic wait-for relations.

- the robot  $R_i$  uses the dependency set  $Depend_i$  to construct  $Dag_{wait}$ . The vertices represent the robots of the set  $Depend_i$  and a directed edge from the robot  $R_i$  to  $R_j$  means that the robot  $R_i$  waits for  $R_j$ .

### The build the wait-for graph $Dag_{wait}$

$Dag_{wait}$  is built as follows. The robot  $R_i$  starts by establishing the imposed wait-for relations and then it breaks links for the remainder of the conflicting robots by the Conflict Resolver.

- At first, the robot  $R_i$  builds the *WAITFORME* graph, denoted  $Dag_{wm}$ . This graph corresponds to the relation between the robot  $R_i$  and  $R_j$  from the set  $(G_1)_i$ .
- The next step, the robot  $R_i$  builds  $Dag_{pg}$  by adding the directed boundaries imposed by the conflict intersection situations.
- After having established the imposed wait for relations, the robot  $R_i$  adds the directed boundaries that result from resolving the conflicts according to a specified policy. The conflicting robots build the directed acyclic graph  $Dag_{wait}$  in a consistent manner.
- According to the graph  $Dag_{wait}$ , the robot  $R_i$  determines  $Before_i$  the set of robots that the robot  $R_i$  waits for. The robot  $R_i$  dynamically updates the set  $After_i$  by adding robots  $R_k$  that does not belong to  $G_i$  and whose requested zone  $Z_k$  intersects with  $Z_i$ . (the robot  $R_i$  sends to  $R_k$  the message  $mssg_i = (WAITFORME, i, Z_i)$ ). The robot  $R_i$  keeps updating the set  $After_i$  until the robot  $R_i$  releases  $Z_i$ .
- The robot  $R_i$  waits until it receives a release message from each robot in the set  $Before_i$ .

3) *Reservation phase*. When the robot  $R_i$  has received a release message from all the robots of the set  $Before_i$ , or (when the set  $Before_i$  is empty), the robot  $R_i$  reserves  $Z_i$  and becomes the owner of  $Z_i$ .

4) *Release phase*. When the robot  $R_i$  reaches the post-motion zone  $post(Z_i)$ , it releases  $Z_i$  except the place that  $R_i$  occupies.  $R_i$  multicasts a release message to all the robots that belong to the set  $After_i$ . These robots are within one communication loop with respect to  $R_i$ , due to the reservation range property.

Therefore, the robots of the set  $After_i$  can receive the release message of  $R_i$ .

## 5. Conflict Resolution Algorithm

The Conflict-Resolver determines the wait-for relation between two conflicting robots according to a conflict resolution policy, if there is no imposed wait for relation between the two robots [5].

A conflict resolution policy can be as follows: the robot  $R_i$  waits-for  $R_j$  if the number of the previous requested zones by  $R_i$  is higher than that of  $R_j$ . The conflict resolution policy is specified by the robotic application. For example, the robot farther to the intersection zone waits-for the closer one, and in case of an equidistance situation, their identifiers are used to break the symmetry [6].

The Conflict Resolver generates the graph  $Dag_{wait}$  by breaking secure between each pair of the robots of the dependency set  $Depend_i$ . The graph  $Dag_{wait}$  is generated in a consistent manner, such that each robot of the set  $Depend_i$  generates the same graph  $Dag_{wait}$  starting from the graph  $Dag_{pg}$  by adding the directed edges representing the wait-for relations after resolving the conflict between each pair of the conflicting robots. The dependency set is scanned according to the increasing order of the identifiers of robots and the conflict resolution policy is applied. If adding a directed edge creates a cycle, then the new directed edge is reversed to break the cycle.

## 6. Conclusions

This protocol is time-free, in the sense that it never relies on physical time, which makes it extremely robust with regard to timing uncertainty common in wireless networks. It requires neither initial nor complete knowledge of the composition of the group, and it relies on a neighborhood discovery primitive which is readily available through most wireless communication devices. It guarantees that no two robots ever collide, regardless of the respective activities of the robots. When moving along a path, the robot's gripper repeats this procedure for each corridor along the path.

The design of the protocol yields scalability due to its locality-preserving property.

Therefore, the protocol can handle a large-sized dynamic group of cooperative robots, situated in a limited transmission range.

The collision prevention protocol was developed to be used in a managed network with a centralized controller that coordinates the communication schedule for the network. A managed network has the prime benefit that each channel in the range can be used without concern for collisions of robots' grippers. Standards specify packet formats and layered transaction models for the wirelessly communication and how multi routes are maintained to a management application. It remains the duty of the network designer to assign data flows based on service requests and reports on how successful the wireless paths have been. The protocol is intended for industrial automation where applications are extremely performance-sensitive; the adoption in this regime will come only after extensive evaluation.

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